Coupled reliability model of biodeterioration, chloride ingress and cracking for reinforced concrete structures

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Abstract

Maintaining and operating civil infrastructure systems has been recognized as a critical issue worldwide. Among all possible causes of safety reduction during the structural lifetime, deterioration is particularly important. Structural deterioration is usually a slow time-dependent process controlled by safety and operation threshold specifications. This paper presents a model of RC deterioration by coupling biodeterioration (i.e., chemical, physical and mechanical action of live organisms), steel corrosion, and concrete cracking. The final purpose of the model is to compute the reduction of the concrete section and the area of steel reinforcement in order to assess the change of structural capacity with time. Given the uncertainties in both the parameters and the model, the probabilistic nature of loads, the material properties and the diffusion process are taken into account to evaluate structural reliability. The model is illustrated with an example where the inelastic behavior of a pile subject to random loading is considered. The results of the analysis have shown that the effect of biodeterioration on the structural performance is significant and can cause an important reduction of its lifetime. On the whole, the paper states that modeling the effects of biodeterioration in RC structures should be included as part of infrastructure planning and design, especially, when they are located in aggressive environments.

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1. Introduction

Civil infrastructure systems are critical assets for any country’s socioeconomic development. Designing these systems for a particular service lifetime and maintaining them in operation has been recognized as a critical issue worldwide. The life-cycle of a structure can be thought of as the time during which the structure is able to meet specific technical requirements with an acceptable level of safety. In life-cycle analysis, the tech-
nical problem focuses on defining the interaction among three main processes: (1) the structural deterioration (e.g., aging, obsolescence), (2) the occurrence of unexpected extreme events (e.g., earthquakes, floods); and (3) the maintenance/rehabilitation program [1]. This paper will focus only on the first aspect. Nowadays, many deteriorated structures are evaluated for possible repair and continued service because they are in a situation where their replacement would be economically unfeasible. Thus, developing robust models for prediction and strategies for periodic inspection and maintenance play a significant role in enabling target reliabilities to be met over a period of continued service [6,7].

Deterioration is common in structures located in aggressive environments and subject to, for instance, sulfate attack, chloride penetration and biodeterioration. Numerous studies have addressed the problem of chloride ingress in concrete structures. However, in addition to chloride penetration, biological processes can accelerate the degradation process by modifying severely the structural durability and reliability. This aspect is particularly important in marine structures (e.g., ports and offshore platforms), sewage systems and waste water treatment plants [2–4].

The cause of failure of reinforced concrete (RC) structures subject to deterioration is a loss of capacity resulting from a combination of steel corrosion and concrete cracking. Corrosion leads to a loss of the effective area of the reinforcement and has proven to be a common cause of failure. In a study conducted by CC Technologies Laboratories Inc. in 2001 [5], it was found that the total direct cost of corrosion in USA is close to US$ 137.9 billion/year. The industrial and infrastructure sectors more susceptible to corrosion damage are shown in Table 1. On the other hand, concrete cracking is the result of many factors among which loading, steel corrosion and the action of live organisms are of particular interest.

Structural deterioration is usually a slow time-dependent process controlled by a safety/operation threshold specification. In RC structures, cover reduction is caused by the joint action of live organisms and the accumulation of large amounts of chlorides and carbon dioxide on the structure surface. As concrete cover is the principal mean of protection from corrosion, live organisms facilitate the diffusion process by eroding the concrete surface and destroying the concrete microstructure. This accelerates time to corrosion initiation and increases the corrosion rate. Predicting the deterioration of RC structures due to chloride penetration when accelerated by live organisms depends on many factors. It is first necessary that the chloride and carbon dioxide concentration on the structural surface becomes high enough. Besides, it is required that the environment provides conditions for live organisms to survive and to carry out their vital processes, i.e., appropriate climate conditions, temperature, light intensity, oxygen availability, surface roughness and so forth. Biodeterioration of concrete structures is a subject that requires further analytical and experimental investigation.

This paper presents a work on modeling RC deterioration by coupling biodeterioration (i.e., action of live organisms), steel corrosion, and concrete cracking. The final purpose of the model is to compute the reduction of the concrete section and the area of steel reinforcement in order to assess the change of structural capacity with time. Given the uncertainties in both the parameters and the model, the probabilistic nature of loads, the material properties and the diffusion process are taken into account to evaluate structural reliability. The RC deterioration is discussed in Section 2, reinforcement corrosion induced by chloride ingress is treated in Section 3 and the proposed model is presented in Section 4. Finally, as an illustrative example, the model has been applied to evaluate the inelastic performance of RC piles located in aggressive environments.

<table>
<thead>
<tr>
<th>Industrial sector</th>
<th>Cost of corrosion 2001 (US$Billion/year)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gas and liquid transmission pipelines</td>
<td>7.0</td>
</tr>
<tr>
<td>Hazardous materials storage</td>
<td>7.0</td>
</tr>
<tr>
<td>Highway bridges</td>
<td>8.3</td>
</tr>
<tr>
<td>Waterways and ports</td>
<td>0.3</td>
</tr>
<tr>
<td>Drinking water and sewer systems</td>
<td>36.0</td>
</tr>
<tr>
<td>Transportation</td>
<td>29.7</td>
</tr>
<tr>
<td>Defense and nuclear waste storage</td>
<td>20.1</td>
</tr>
<tr>
<td>Production and manufacturing</td>
<td>17.6</td>
</tr>
<tr>
<td>Others</td>
<td>11.9</td>
</tr>
<tr>
<td>Total</td>
<td>137.9</td>
</tr>
</tbody>
</table>

Table 1
Cost of corrosion in several industrial and infrastructure sectors
2. Reinforced concrete deterioration

2.1. Cracking and corrosion

In optimal conditions, the durability of RC structures is high and the variation of the structural reliability with time is not significant. However, for special structures located in aggressive environments this might not be the case. Some examples of aggressive environments are those in which there is:

1. high relative humidity (i.e., between 60% and 98%);
2. cycles of humidification and drying, of freezing and defrosting;
3. high carbon dioxide concentrations (e.g., carbonation in urban atmospheres);
4. high concentration of chlorides or other salts (e.g., marine environments); or
5. high concentration of sulfates and small amounts of acids (e.g., sewer pipes or residual water treatment plants).

In any deterioration process, the structural reliability becomes a time-dependent process; for the particular case of chloride penetration leading to steel corrosion in RC structures, this process has been widely studied. The time-dependent reliability problem is described schematically in Fig. 1. The structure life-cycle can be divided into three stages [8,9]:

- **Stage 1**: after construction structural reliability is maximum; then, deterioration initiates as a result of the environmental conditions such as: chloride ingress, carbonation, sulfate attack, biodeterioration, erosion, etc. Nevertheless, the consequences of these actions do not have a significant impact on the reliability until their individual or joint actions create the necessary conditions to depassivate the protective layer of the steel, e.g., low pH of concrete, optimal temperature, water and oxygen. As a result of this new state, the reinforcement corrosion starts; this time is called *time to corrosion initiation* (*τ*\textsubscript{ini}) (see also Fig. 2a).

- **Stage 2**: as soon as corrosion starts, corrosion products appear. Since these products have a lower density, they occupy the porous zone of concrete around the steel. When the total amount of corrosion products exceeds the amount needed to fill the porous zone, an expansive pressure is induced on the concrete initiating the cracking process [10,11]. In this stage, two phenomena called crack initiation and crack propagation are present. The former is defined as the condition for which a hairline crack of 0.05 mm width appears [12,13]. The time required to reach this point is called *time to crack initiation* (*τ*\textsubscript{cr}) (Fig. 2b). The latter is the process that follows crack initiation and it is measured in terms of the crack width, *cw*. The time required to reach the threshold crack size, *cw*\textsubscript{lim} (e.g., *cw*\textsubscript{lim} = 0.5 mm) is called *time to severe cracking* (*τ*\textsubscript{sp}). Once this stage is reached, reliability reduces playing an important role in the structural safety.

![Fig. 1. Reliability profile for RC structures subject to corrosion.](image-url)
Stage 3: when crack width reaches the threshold value, there is a significant increment of the corrosion rate as a result of an increase in water and oxygen availability and in concrete electrical conductivity [14]. This accelerated increase reduces safety significantly.

2.2. Biodeterioration

The process of deterioration of RC structures as a result of the action of live organisms (chemical and physical) is usually called concrete biodeterioration. Biodeterioration was defined by Hueck [15] as: “...any undesirable change produced by normal activities of live organisms on materials”. According to Gaylarde [16], biodeterioration can be classified within three types:

- **Aesthetic**: it is concerned with the presence of microorganisms on the surface of the structure producing a disagreeable aspect.
- **Chemical**: it refers to the degradation of cement and aggregates as a result of substances emanated by live organisms.
- **Physical**: it encompasses all physical actions of organisms leading to a physical deterioration of RC.

Biodeterioration is caused by live organisms that can be found in the ground, the water or the air. In many cases, they can be found on concrete surfaces that offer favorable conditions for them to survive; for example, places where the surface texture allows them to settle down, there is water available, the pH of concrete is low, the temperature conditions are appropriate and where there are nutrients for their survival. When these organisms settle on the concrete surface, they form a film called biofilm, which is followed by the chemical biodeterioration of concrete.

Biodeterioration is caused mainly by: (1) bacteria; (2) fungi; (3) algae and lichens; and (4) organisms that erode and drill the concrete [17].

2.2.1. Bacteria

They are unicellular microorganisms with size of one micron or less. They can be classified as autotrophic or heterotrophic; also, they can be aerobe, anaerobe or aerotolerant anaerobes (see Appendix A for definitions). Among those that cause concrete deterioration some of the most important are: (1) cyanobacteria; (2) nitrobacteria; (3) sulfur-reducing bacteria; and (4) sulfur-oxidizing bacteria. Their main characteristics are presented in Table 2.

The chemical action of cyanobacteria does not affect RC considerably, however, its organic material secretion serves as nutrient for fungi and heterotrophic bacteria that can be very aggressive to RC. Regarding the
physical degradation, the endolithic cells penetrate in concrete through micro-cracks absorbing water, which causes a growth of their molecular mass generating tensile stresses leading to an increment in the size of cracks [16].

Nitrobacteria transform ammonia from the atmosphere into nitrites and nitrates; this process is called nitrification. Nitrites and nitrates attack the concrete and as a result of the reaction, “calcium nitrate” is produced. It affects the concrete since it results from the solubilization of the cement components [18–21].

Sulfur-reducing bacteria oxidize the sulfate existing in the water and transform it into hydrogen sulfides and H$_2$S in gaseous state. It does not affect the concrete directly; nevertheless, the H$_2$S is used for the sulfur-oxidizing bacteria to produce sulfuric acid. This process is commonly called concrete corrosion. It can be found frequently in closed structures such as: sewage systems and waste water treatment plants.

Sulfur-oxidizing bacteria are divided in two groups: (1) neutrophilic sulfur oxidizing microorganisms (NSOM); and (2) the acidiphilic sulfur oxidizing microorganisms (ASOM). The oxygen required for their existence causes that they oxidize the H$_2$S (produced by the sulfur-reducing bacteria), transforming it into sulfuric acid H$_2$SO$_4$, which reacts with the cement forming calcium sulfate (gypsum). Furthermore, when gypsum is combined with the hydrated aluminate of calcium, it forms sulfur-aluminate of calcium (ettringite). In addition, it can produce acetic acid, sulfates, sulfur, sulfites and polythionates, substances that affect the concrete chemically. Roberts et al. [24] report five species of this bacteria called Thiobacillus; their main characteristics are shown in Table 3. The first four species are NSOM and the last is ASOM. The last species (i.e., *T. thiooxidans*) are the group of microorganisms that causes more damage to concrete. Table 4 shows some values of concrete biodeterioration rates as a result of the action of ASOM.

**Table 2**
Effects of bacteria on RC structures

<table>
<thead>
<tr>
<th>Bacteria type</th>
<th>Lifestyle</th>
<th>Temperature and pH range</th>
<th>Consequences on concrete</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. Cyanobacteria</td>
<td>Autotrophic, aerobe or anaerobe</td>
<td>−60 to 85 °C (wide range pH)</td>
<td>Generate tensile stresses leading to an increment in the size of cracks.</td>
</tr>
<tr>
<td>2. Nitrobacteria</td>
<td>Heterotrophic and anaerobe</td>
<td>18–25 °C, pH &lt; 7.5</td>
<td>Nitrifying bacteria (Nitrosomonas and Nitrobacter) produce calcium nitrate by solubilising some of cement components.</td>
</tr>
<tr>
<td>3. Sulfur-reducing bacteria</td>
<td>Heterotrophic and anaerobe</td>
<td>25–44 °C, 5.5 &lt; pH &lt; 9</td>
<td>Produce H$_2$S that is used for the sulfur-oxidizing bacteria to produce sulfuric acid. This process is commonly called concrete corrosion.</td>
</tr>
<tr>
<td>4. Sulfur-oxidizing bacteria</td>
<td>Heterotrophic and aerobe</td>
<td>25–44 °C, 2 &lt; pH &lt; 9</td>
<td>Produce sulfuric acid, acetic acid, sulfates, sulfur, sulfites and polythionates that affect the concrete chemically.</td>
</tr>
</tbody>
</table>

Nitrobacteria transform ammonia from the atmosphere into nitrites and nitrates; this process is called nitrification. Nitrites and nitrates attack the concrete and as a result of the reaction, “calcium nitrate” is produced. It affects the concrete since it results from the solubilization of the cement components [18–21].

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**Table 3**
Five species of Thiobacillus and their characteristics

<table>
<thead>
<tr>
<th>Species</th>
<th>pH range</th>
<th>Lifestyle</th>
<th>Products</th>
</tr>
</thead>
<tbody>
<tr>
<td><em>T. thioparus</em></td>
<td>4.5–10</td>
<td>Autotrophic aerobe</td>
<td>Sulfur, polythionic acids</td>
</tr>
<tr>
<td><em>T. novellus</em></td>
<td>5–9.2</td>
<td>Mixotroph</td>
<td>Sulfur</td>
</tr>
<tr>
<td><em>T. neapolitanus</em></td>
<td>4–9</td>
<td>Autotrophic</td>
<td>Polythionic acids, sulfuric acids</td>
</tr>
<tr>
<td><em>T. intermedius</em></td>
<td>1.7–9</td>
<td>Mixotroph</td>
<td>Polythionic acids, sulfuric acids</td>
</tr>
<tr>
<td><em>T. thiooxidans</em></td>
<td>0.5–4</td>
<td>Autotrophic</td>
<td>Sulfur, sulfuric acids</td>
</tr>
</tbody>
</table>
2.2.2. **Fungi**

Fungi can be found almost everywhere (even in adverse atmospheres with little water and without air) as long as there is organic matter available. Generally, they survive in temperatures between 25 and 30 °C. Usually, fungi found in RC surfaces are simple fungi, mold, and yeast [3]. They produce mechanical damage in the concrete micro-structure by the hyphae penetration. In addition, they deteriorate concrete chemically by the generation of organic and inorganic acids that precipitate salts.

2.2.3. **Algae and lichens**

The algae are a complex and varied vegetal group, for this reason their description and classification is not an easy task. They can survive in any habitat where there are both light and humidity; then, they can be found in the sea, humid soils, and snow. Their action on concrete structures consists on taking calcium, magnesium, and silica, for their metabolic processes, from the cement paste generating small cavities in the concrete.

Lichens are the product of the symbiosis of an alga and a fungus. The fungus provides water to alga, and the alga takes from the fungus inorganic substances; then, they complement each other to survive in very hostile environments. On concrete surfaces colonized by lichens there can be found many micro-perforations with diameters between 0.5 and 10 µm as well as perforations with diameters between 0.1 and 0.5 mm [2].

2.2.4. **Organisms that erode and drill the concrete**

When concrete biodeterioration is not controlled, a series of organisms of appreciable size appears [2]. These types of organisms are found generally in tropical environments and on the concrete surface, where the biofilm has been formed. Between the organisms that erode concrete, the most representative are the mollusk [28] whose action consists on continuously scrape the surface. Among the second class of organisms, there are the bivalves, the crustaceans and the sipunculids [28]. They make perforations of cavern type by means of chemical and physical processes.

2.2.5. **Biodeterioration control measures**

There are many preventive measures to control the action of live-organisms which depend basically on the characteristics of the species and the environmental conditions. Any procedure of counter-measures to diminish or mitigate damage must include the following actions: (1) to establish a regime of inspection or monitoring that detects immediately the appearance of the biofilm; (2) to determine the organisms that constitute the biofilm, including its density and location; (3) to elaborate an integrated plan against the involved organisms in order to solve the problem, and (4) to supervise the integrated plan and its results. Depending on the type of organism detected (i.e. step two) and the degree of damage of the structure, the integrated plans can include a combination of the following measures: (1) surface cleaning using chemical agents (i.e. biocides), biological and physical means; (2) surface painting using admixtures with biocides; and (3) replacement of concrete cover. Specific information on these counter-measures is beyond the scope of this paper, but they can be found in the literature [29–32].

3. **Corrosion of steel reinforcement**

In addition to concrete biodeterioration, RC structural integrity may be seriously affected by steel corrosion. Steel corrosion caused by chloride ingress has been widely studied and some basic concepts are presented in this section. Tuutti [33] proposed a model of the ingress of chlorides in concrete as function of time and depth using the Frick’s second law of diffusion,
\[ \frac{\partial C}{\partial \tau} = D_{cl} \frac{\partial^2 C}{\partial x^2}, \]  

where \( C \) is the chloride ion concentration, \( D_{cl} \) is the chloride diffusion coefficient in concrete, \( \tau \) is the time and \( x \) is depth in the diffusion direction. Assuming that concrete is an homogenous and isotropic material with the initial conditions: (1) when time is zero, the concentration is zero and (2) the chloride surface concentration is constant, then, the chloride ion concentration, \( C(x, \tau) \), at depth \( x \) after time \( \tau \) is:

\[ C(x, \tau) = C_s \left[ 1 - \text{erf} \left( \frac{x}{2 \sqrt{D_{cl} \tau}} \right) \right], \]

where \( C_s \) is chloride surface concentration and \( \text{erf} \) is the error function.

The threshold concentration, \( C_{th} \), is defined as the chloride concentration for which the rust passive layer of steel is destroyed and the corrosion reaction begins, that instant is called time to corrosion initiation \( \tau_{ini} \). From Eq. (2), when \( C(x, \tau) \) is equal to \( C_{th} \) and \( x \) is equal to the bar cover \( c \), \( \tau_{ini} \) is computed as:

\[ \tau_{ini} = \frac{c^2 \left( \text{erf}^{-1} \left( 1 - \frac{C_{th}}{C_s} \right) \right)}{4D_{cl}}. \]

The depth of threshold concentration \( C_{th} \) at time \( \tau \) called “penetration depth of chloride threshold aggressive front” \[34\] \( D_{th}(\tau) \) is obtained if the concentration \( C(x, \tau) = C_{th} \) and \( x = D_{th}(\tau) \), then, Eq. (2) becomes:

\[ D_{th}(\tau) = 2\sqrt{D_{cl} \tau} \text{erf}^{-1} \left( 1 - \frac{C_{th}}{C_s} \right). \]

At time \( \tau \), the corrosion density, \( i_{corr}(\tau) \), is expressed according to the Faraday’s law as:

\[ i_{corr}(\tau) = J_c(\tau)n_{O_2}F, \]

where \( n_{O_2} \) is the obtained electric number of \( O_2 \) molecule participated in chemical reaction (\( n_{O_2} = 4 \)), \( J_c(\tau) \) is the diffusion flow of \( O_2 \) in concrete at time \( \tau \) and \( F \) is Faraday’s constant, \( F = 96,500 \) C/mol. On the other hand, based on electrochemistry principles, the diffusion flow of \( O_2 \) in concrete is equal to \[35\]:

\[ J_c(\tau) = D_{O_2} \frac{\partial C(x)}{\partial x}, \]

where \( D_{O_2} \) is the diffusion coefficient of \( O_2 \) in the concrete (mm\(^2\)/year) and \( x \) is the coordinate space in the diffusion direction. According to the Frick’s diffusion law there is a linear variation of the oxygen concentration. Therefore, if the oxygen concentration on the surface is \( C_{O_2} = 8.93 \times 10^{-10} \) mol/mm\(^3\) and at the depth \( D_{th}(\tau) \) the concentration is \( C_{st} = 0 \) [35]:

\[ \frac{\partial C(x)}{\partial x} = \frac{C_{O_2} - C_{st}}{D_{th}(\tau)}. \]

Replacing Eqs. (6) and (7) into Eq. (5) yields to:

\[ i_{corr}(\tau) = \frac{n_{O_2}F D_{O_2} C_{O_2}}{D_{th}(\tau)}. \]

On the other hand, according to Faraday’s law, the product of steel corrosion during time \( d\tau \) is:

\[ dW_c = \frac{i_{corr}(\tau)}{n_a F} MA_s(\tau) d\tau, \]

where \( dW_c \) is the amount of corrosion products in grams at time \( d\tau \), \( M \) is the atomic weight of Fe (M = 55.85 g/mol), \( n_a \) is the electric charge of iron ion (\( n_a = 2 \)) and \( A_s(\tau) \) is the corrosion surface area of steel in concrete at time \( \tau \) considering a 1 mm unit length bar (Fig. 2), and is equal to:

\[ A_s(\tau) = d \cos^{-1} \left( \frac{d + 2c - 2 D_{th}(\tau)}{d} \right). \]
where \(d\) is the initial bar diameter in mm and \(c\) is the cover thickness in mm. Niu et al. [36] proposed an equation for calculating \(D_{O_2}\) as a function of the concrete compressive strength \(f'_{cu}\) in N/mm\(^2\) (\(f'_{cu}\) is obtained from the test over a concrete cube sample):

\[
D_{O_2} = 3.1536 \times 10^5 \left( \frac{32.15}{f'_{cu}} - 0.44 \right) \left[ \frac{\text{mm}^2}{\text{year}} \right].
\]  

(11)

If \(\tau_w\) is the time to full corrosion, this occurs when \(A_s(\tau) = \pi d\), then, for \(\tau_w \geq \tau\), the amount of corrosion products, \(W(\tau)\), is obtained by replacing Eq. (8) into Eq. (9) and integrating with respect to time:

\[
W(\tau) = \begin{cases} 
0 \text{ grams} & \text{if } \tau_{ini} \geq \tau \\
kd_{O_2} \int_{\tau_{ini}}^{\tau} \frac{d_{s}(\tau)}{D_{th}(\tau)} \, d\tau & \text{if } \tau_{w} \geq \tau > \tau_{ini} 
\end{cases}
\]

where \(k = n_{O_2} C_{O_2} M / n_a = 7.125 \times 10^{-8} \text{ g/mm}^3\). Finally, if \(\tau > \tau_w\), \(A_s(\tau) = \pi d\) and \(D_{th}(\tau) = c + d\), then,

\[
W(\tau) = \begin{cases} 
0 \text{ grams} & \text{if } \tau_{ini} \geq \tau \\
kD_{O_2} \int_{\tau_{ini}}^{\tau} \frac{d_{s}(\tau)}{D_{th}(\tau)} \, d\tau & \text{if } \tau_{w} \geq \tau > \tau_{ini} \\
kD_{O_2} \left( \int_{\tau_{ini}}^{\tau_w} \frac{d_{s}(\tau)}{D_{th}(\tau)} \, d\tau + \frac{\pi d}{c + d} \int_{\tau_{w}}^{\tau} \, d\tau \right) & \text{if } \tau > \tau_w
\end{cases}
\]

(13)

Based on Eq. (13), it is then possible to compute the effective diameter of the bar as function of time as follows:

\[
d_{bar}(\tau) = d_0 \left( 1 - \frac{W(\tau)}{W_0} \right),
\]

(14)

where \(d_{bar}(\tau)\) is the diameter of the bar at time \(\tau\), \(d_0\) is the bar initial diameter, \(W(\tau)\) is the amount of corrosion products in (g) by 1 mm of length at time \(\tau\) calculated by Eq. (13) and \(W_0\) is the bar initial weight in (g) by 1 mm length.

4. Coupled deterioration model

The coupled model presented in this section takes into account three effects (Fig. 3): (1) corrosion induced by chloride ingress; (2) cracking as a result of corrosion products; and (3) reduction of concrete cover caused by biodeterioration. In the first part of this section, the corrosion model presented in the previous section will be modified to include the effect of cracking. Afterwards, a time-dependent biodeterioration rate function is obtained by using a fuzzy logic inference system. Finally, all three effects are coupled into one single model.

4.1. RC cracking as a result of corrosion products

Once corrosion starts there are stresses resulting from the expansion produced by corrosion. Then, in order to take into account this effect, Liu and Weyers [11] proposed a model to find the time to crack initiation, \(\tau_{cr}\), that is a function of the amount of rust products. They defined the amount of critical rust products \(W_{crit}\) (g) as the amount for which all free spaces between the steel bar and the concrete are filled and the cracking begins. It can be calculated as:

\[
W_{crit} = \frac{\rho_{steel}}{\rho_{steel} - 0.57 \rho_{rust}} (W_{porous} + W_{Expand}),
\]

(15)

where \(\rho_{steel}\) is the density (g/mm\(^3\)) of reinforced steel, \(\rho_{rust}\) is the density of corrosion products, \(W_{porous}\) is the amount of corrosion products necessary to fill the porous zone around the steel/concrete interface and is defined as:

\[
W_{porous} = \pi \rho_{rust} t_{por} d,
\]

(16)
where $t_{\text{por}}$ is the thickness of porous band around the steel concrete interface and $d$ is the diameter of the steel bar. Besides, $W_{\text{Expand}}$ is the amount of corrosion products needed to fill in the space due to the expansion of the concrete around the reinforcement; this is:

$$W_{\text{Expand}} = \pi \rho_{\text{rust}} (d + 2t_{\text{por}}) t_{\text{crit}},$$

where $t_{\text{crit}}$ is the thickness of corrosion products needed to generate the tensile stresses [11] and it is computed as:

$$t_{\text{crit}} = \frac{cf_0^t}{E_c} \left( \frac{k^2 + l^2}{l^2 - k^2} + v_c \right),$$

where $f_0^t$ is the tensile strength of concrete, $E_c$ is the elastic modulus of concrete, $k = (d + 2t_{\text{por}})/2$, $l = c + (d + 2t_{\text{por}})/2$ and $v_c$ is Poisson’s ratio of concrete.

Fig. 3. Conceptual description of the coupled model for biodeterioration, chloride ingress and cracking of concrete structures.

Fig. 4. (a) Change of the amount of corrosion products and the diameter of the steel bar with time; (b) variation of the diffusion oxygen coefficient with time.
The amount of corrosion products $W(\tau)$ is zero if the age of the concrete $\tau$ is less than $\tau_{\text{ini}}$ (Fig. 4a). When $\tau \leq \tau_{\text{sp}}$, the value of $D_{O_2}$ is obtained by using Eq. (11). The time to severe cracking, $\tau_{sp}$, is equal to [12,13]:

$$\tau_{sp} = \tau_{cr} + \tau_{pr},$$

where $\tau_{sp}$ is the time to crack propagation. Based on experimental data obtained from accelerated corrosion tests with a corrosion rate of $i_{\text{corr(acc)}} = 100 \mu A/cm^2$, Vu et al. [13] found that the accelerated time to crack propagation in hours can be estimated as:

$$\tau_{pr(acc)} = \frac{\xi}{c} (w/c)^{s},$$

where $c$ is the cover in mm, $w/c$ is the water/cement ratio, and $\xi$ and $\lambda$ are parameters that depend on the limit crack width. For instance, when $cw_{\text{lim}} = 0.5$ mm, $\xi = 225$ and $\lambda = 0.29$ [13]. Since Eq. (20) was obtained from accelerated tests, a correction factor, $k_R$, has been deduced by Vu et al. [13], based on the experimental values obtained by Alonso et al. [37] as:

$$k_R \approx 0.95 \left[ \exp \left( -\frac{0.3i_{\text{corr(acc)}}}{i_{\text{corr(real)}}} \right) - \frac{i_{\text{corr(acc)}}}{2500i_{\text{corr(real)}}} + 0.3 \right],$$

where $i_{\text{corr(real)}}$ corresponds to the real corrosion rate in $\mu A/cm^2$. Therefore, the time to crack propagation in years is:

$$\tau_{pr} = k_R \frac{0.0114}{i_{\text{corr(real)}}} \tau_{pr(acc)}.$$  

After cracking begins (i.e., $\tau > \tau_{sp}$), the diffusion coefficient $D_{O_2}$ becomes time-dependent and a linear behavior is assumed. Consider that at time $\tau_n$ (with $\tau_n \gg \tau_{sp}$; e.g. $\tau_n = 500$ years) the oxygen concentration at the steel surface (i.e., $C_{O_2}$) is closer to the oxygen concentration at the concrete surface $C_{O_2}$ (i.e., $C_{O_2} \approx C_{O_2}$). Then substituting these values into Frick’s second law (Eq. (2)), it is possible to compute a new oxygen diffusion coefficient at time $\tau_n$, as:

$$D_{nO_2}(\tau_n) = \frac{c^2}{4\tau_n \left[ \text{erf}^{-1} \left( 1 - \frac{C_{O_2}}{C_{O_2}} \right) \right]^2},$$

and the diffusion coefficient of oxygen in the concrete ($DC_{O_2}$) at time $\tau$ becomes (Fig. 4b):

$$DC_{O_2}(\tau) = \begin{cases} D_{O_2} & \text{if } \tau \leq \tau_{sp} \\ D_{O_2} + \frac{(D_{O_2} - D_{O_2})}{(\tau - \tau_{sp})} (\tau - \tau_{sp}) & \text{if } \tau > \tau_{sp} \end{cases}$$

then, by substituting Eq. (24) into (13), the amount of corrosion products when considering the RC cracked, $W_{\text{crack}}(\tau)$, in (g) by 1 mm of length at time $\tau$ is given by:

$$W_{\text{crack}}(\tau) = \begin{cases} 0 \text{ grams} & \text{if } \tau_{\text{ini}} \geq \tau \\ k \int_{\tau_{\text{ini}}}^{\tau} DC_{O_2}(\tau) d\tau & \text{if } \tau_{\text{w}} \geq \tau > \tau_{\text{ini}} \\ k \left( \int_{\tau_{\text{ini}}}^{\tau} DC_{O_2}(\tau) d\tau + \frac{m_{O_2}}{c+dl} \int_{\tau_{\text{w}}}^{\tau} DC_{O_2}(\tau) d\tau \right) & \text{if } \tau > \tau_{\text{w}} \end{cases}$$

The consequences of cracking on the corrosion rate are not easy to evaluate; Fig. 5 presents several models. In the first model, the time-variant corrosion rate has been computed by using the values reported by Vu et al. [13]. In this model, corrosion rate remains constant during the first year, after which, the formation of rust products on the steel surface reduces this rate substantially. The second model considers a reduction of corrosion rate, from the time to corrosion initiation ($\tau_{\text{ini}}$) until the time to full corrosion ($\tau_{\text{w}}$). After this point, the corrosion rate remains constant. In the third case, the model includes concrete cracking and assumes that the change of the diffusion coefficient of concrete (Eq. (20)) begins only after the time to crack initiation ($\tau_{cr}$). After this point, diffusion grows due to the increase in the diffusion oxygen coefficient. The last case is similar to the previous one but the effect of cracking has only an important impact when the crack width reaches a limit value of $cw_{\text{lim}} = 0.5$ mm ($\tau_{sp}$). In this case, the corrosion rates are lower than in the third case (see also Fig. 4).
The first two models presented in Fig. 5 do not take into account concrete cracking to estimate corrosion rate, while the last two do. In this paper the last model was used to compute the amount of corrosion products. It is important to note that the corrosion rates used in this paper are within the range suggested by EN 206 [38] for corrosion induced by chloride ingress in tidal zones.

4.2. Time-dependent biodeterioration rate function

Biodeterioration is a very complex process where many classes of organisms, environmental variables and other deteriorating processes interact. Computing the RC time-dependent biodeterioration rate is a crucial aspect for the accuracy of the numerical model. However, to the authors knowledge, no much work has been done in this field and there is not yet a robust model of this process. As no sufficient data are available to perform appropriate statistical analysis, the application of probability theory is not possible. Thus, non precise data is considered based on existing experimental reports (Table 1). The proposed model is based on fuzzy inference, which is a valuable tool for managing situations where information about a process can only be described conceptually or there is not enough data to build a robust statistical model. Then, based on fuzzy logic, a model to obtain a time-dependent function of the biodeterioration rate is proposed.
Conceptually, the process can be divided into three stages (Fig. 6):

1. **RC immunity**: in this stage, due the concrete high alkalinity (pH between 11 and 13), the organisms cannot survive nor adhere to it; therefore, the RC is immune to biological damage.
2. **Biofilm formation**: the presence of CO₂ in the atmosphere causes carbonation, which in turn leads to a reduction of the pH of the RC surface (until approximately 9). In addition, the erosive action of the water and/or the friction with other materials generate certain roughness on the concrete surface that allows microorganisms to adhere forming the biofilm. Experimental evidence has shown that microorganisms can also ingress into concrete by a diffusion process altering the concrete microstructure [39].
3. **Active biodeterioration of concrete**: in this stage, the concrete pH continues decreasing, by the joint action of carbonation and organisms until it reaches a value of pH < 5. The RC surface is highly deteriorated and the cracks have an important size. All those conditions make possible that other organisms also stick to biofilm on the surface contributing to RC chemical deterioration. When the concrete is cracked, some organisms like the endolithic cells, algae and fungi ingress into cracks, generating tensile stresses that deteriorate the concrete by increasing the crack size. Crack formation can also be promoted as a result of the weakened on the concrete microstructure caused by fungi and other microorganisms that might have already enter into concrete matrix by diffusion.

Based on the conceptual model the membership functions for the age of the structure (i.e., in time units (years), \( \tau \)) and the biodeterioration rate \( \gamma \) (mm/year) can be defined. Then, the structure life can be divided in two stages:

1. **Initial age**: at this age, microorganisms can hardly live on the surface of the concrete because it is even and the pH of concrete is high.
2. **Active biodeterioration age**: at this stage, the biodeterioration is active because the surface offers optimal conditions for colonization of microorganisms.

These stages are represented by membership functions of sigmoidal form (see Fig. 7a): 

\[
\mu_{age}(\tau, a, b) = \frac{1}{1 + \exp(-a(\tau - b))}, \tag{26}
\]

where \( \tau \) is the time in years and \( a, b \) are constants that define the shape of the function. In addition, it is necessary to define two membership functions for the corresponding biodeterioration rate, \( \gamma \). The first corresponds to the initiation of the biodeterioration process for which the maximum membership value assigned is \( \gamma_{\text{ini}} = 0 \) mm/year. Then, in this case, the modified Gaussian function that describes the initial biodeterioration rate membership is given by (see Fig. 7b):

![Fig. 7. (a) Age membership functions, (b) biodeterioration rate membership functions.](image-url)
where $\sigma$ is a shape parameter. The second function corresponds to the time within which biodeterioration is active; thus, based on the values presented in Table 4, the average active biodeterioration rate, $\gamma_{av}$, is assigned to the maximum membership value. In this case, the membership function that describes the corrosion rate is:

$$
\mu_{c1}(c; \sigma) = \begin{cases} 
\exp \left( -\frac{1}{2} \left[ \frac{c}{\sigma} \right]^2 \right) & \text{if } c \geq 0 \\
0 & \text{otherwise} 
\end{cases},
$$

(27)

Fig. 7 illustrates these functions for the following parameters: $\alpha_{ini} = -0.8$ and $b_{ini} = 6.5$ for the initial age; $\alpha_{act} = 0.7$ and $b_{act} = 12$ for the active biodeterioration age; $\sigma_{ini} = 0.1$ for the initial biodeterioration rate; and $\gamma_{av} = 2.5$ mm/yr and $\sigma_{act} = 0.4$ for the active biodeterioration rate.

The rules used for the fuzzy inference system are:

1. If the structure is in the initial age, then the biodeterioration rate is the initial.
2. If the structure is in the active biodeterioration age, then the biodeterioration rate is active.

Based on these rules a response surface can be determined as follows:

$$
S(\tau, \gamma) = \max \left( \frac{\mu_{age1}(\tau, \alpha_{ini}, b_{ini}) \mu_{c1}(\gamma; \sigma_{ini})}{\mu_{age2}(\tau, \alpha_{act}, b_{act}) \mu_{c2}(\gamma, \gamma_{av}, \sigma_{act})} \right),
$$

(29)

where $S(\tau, \gamma)$ is the surface generated by the maximum of products composition, $\mu_{age1}(\tau, \alpha_{ini}, b_{ini})$ is the membership function corresponding to concrete initial age, $\mu_{age2}(\tau, \alpha_{act}, b_{act})$ to active biodeterioration age, $\mu_{c1}(\gamma; \sigma_{ini})$ to initial biodeterioration rate and $\mu_{c2}(\gamma, \gamma_{av}, \sigma_{act})$ to active biodeterioration rate. The surface generated by Eq. (29) is shown in Fig. 8a. Finally, by using the strategy of the center of gravity for the surface defuzzification, it is possible to obtain a time-dependent biodeterioration rate function, $\gamma(\tau)$, as (Fig. 8b):

$$
\gamma(\tau) = \frac{\int \gamma \cdot S(\tau, \gamma) \, d\gamma}{\int S(\tau, \gamma) \, d\gamma}.
$$

(30)

The advantage of this solution is that it provides an estimation of the time-dependent change of the biodeterioration rate, which depends on the expert’s knowledge. Hence the expert has to define the appropriate conceptual model of the problem as presented above. Moreover, he/she determines the form of the membership functions, since he/she has to assign values to the variables $a$, $b$, $\gamma_{av}$ and $\sigma$ based on his/her expertise. For example, an expert can define the membership functions of the biodeterioration rate considering environmental factors and nutrients availability of determinate place, and the age membership functions taking into

![Fig. 8. (a) Surface generated in FIS type Mamdani, (b) time-dependent biodeterioration rate function.](image-url)
account the type of cement or the condition of the structure at a given time. It is important to stress on the fact that the biodeterioration rate function can be updated permanently by modifying the membership functions based on field measurements and experimental data.

4.3. Coupled model

Due to action of live organisms, the thickness of the concrete cover is a time-dependent function. Then, the thickness at time \( t \) (i.e., \( \text{cover}(t) \)) is calculated as:

\[
\text{cover}(t) = c - \int_{0}^{t} \gamma(t) \, dt,
\]

where \( c \) is the cover at \( t = 0 \) and \( \gamma(t) \) corresponds to the biodeterioration rate function showed in Fig. 8b. Then, the time to corrosion initiation \( \tau_{\text{ini}} \) is calculated by replacing Eq. (31) into Eq. (3),

\[
\tau_{\text{ini}} = \frac{\text{cover}^2(t) \left[ \text{erf}^{-1}(1 - \frac{C_{c}}{C_{0}}) \right]^2}{4D_{\text{cl}}}. \tag{32}
\]

For time \( \tau > \tau_{\text{ini}} \), the advance of the aggressive corrosion front, \( D_{\text{th}}(t) \) (Eq. (4)), and the reduction of steel area grow rapidly affecting considerably the properties of the structural member. Therefore, Eq. (10) is modified simply by making the cover thickness a function of time. That is:

\[
A_{\text{am}}(t) = d \cos^{-1} \left( \frac{d + 2\text{cover}(t) - 2D_{\text{th}}(t)}{d} \right), \tag{33}
\]

where \( A_{\text{am}}(t) \) is the corroded surface area of the reinforcement at time \( t \) (taking 1 mm unit length) when the biodeterioration process is taken into account. Consequently, the amount of corrosion products \( W_{m}(t) \), which is function of \( A_{\text{am}}(t) \), can be expressed as:

---

![Flow diagram describing the coupled model.](image)
\[
W_m(\tau) = \begin{cases} 
0 \text{ grams} & \text{if } \tau_{mi} \geq \tau \\
0 \text{ grams} & \text{if } \tau_{w} \geq \tau > \tau_{mi} \\
k \int_{\tau_{mi}}^{\tau} \frac{D\sigma_o}{D\mu_o} \, d\tau & \text{if } \tau > \tau_{w} \\
\frac{k}{c+D} \int_{\tau_{mi}}^{\tau} D\sigma_o(d\tau) & \text{if } \tau > \tau_{w} 
\end{cases}
\]

(34)

On the whole, the proposed model couples three processes: (1) steel corrosion; (2) concrete cracking; and (3) biodeterioration. The flow diagram that summarizes the entire procedure is presented in Fig. 9. The ultimate purpose of the model is to compute the reduction of steel reinforcement area of the RC element. As it will be shown in the numerical example, this approach to RC biodeterioration can be used to make better estimates of structural reliability and is an important tool for intervention and rehabilitation purposes.

5. Numerical example

5.1. Basic considerations and assumptions

In this section, the coupled model described in the previous section is illustrated with a numerical example. The goal of this example is to compute the probability of failure of a seaport reinforced concrete pile in terms of its curvature ductility capacity. The pile showed in Fig. 10 is part of a port structural system subject to axial loading produced by the loading and unloading of containers on the platform (see Fig. 10a). The port is located in a tropical region where the environmental conditions make the structure susceptible to biological deterioration. The geometric characteristics of the pile are presented in Fig. 10b.

For structures immersed in the sea, there are three zones (see Fig. 10a), with different surface chloride concentration and availability of oxygen and water for which the cinematic of the corrosion process is different [40]. These are: (1) the submerged zone, (2) the splash and tidal zone, and (3) the atmospheric zone. In the first zone, the surface chloride concentration is higher that in the other zones, but the risks of corrosion and biodeterioration are low because the oxygen and light are not available. In the splash and tidal zone, the RC sur-

Fig. 10. Pile configuration: (a) description example, load and zones, (b) pile cross-section.
face is exposed to wetting and drying cycles that provide the optimal conditions (chlorides, water and oxygen) for corrosion to initiate. Furthermore, the existence of light, nutrients and water in sufficient quantities promotes the appearance of the biofilm. It is widely accepted that the highest risks of corrosion and biodeterioration occur in this zone. Finally, in the last region the wind is the main source of chlorides and the water available is low, thus, the risks of corrosion and biodeterioration are small. Therefore, the present example focuses on the splash and tidal zone.

The following assumptions about the problem have been made:

- The density of steel reinforcement is assumed deterministic ($\rho_{\text{steel}} = 8000 \text{ kg/m}^3$).
- The tensile strength of concrete is given by a percentage of its compressive strength (i.e. $f'_{t} = 0.10 f'_{c}$). Perfect correlation between tensile and compressive strengths is assumed.
- In order to estimate the time to severe cracking, a limit crack width of $c_{w,\text{lim}} = 0.5 \text{ mm}$ has been chosen.
- The water/cement ratio is calculated by using the Bolomey’s formula.
- The corrosion of steel is assumed to be uniform.
- The deterioration process is continuous, i.e. there is not maintenance.

5.2. Reliability problem formulation

Ductility capacity is the structural ability to sustain, without failure, deformations well beyond the elastic limit. In this case, the curvature ductility capacity $\mu_{\phi}$ is equal to,

$$\mu_{\phi} = \frac{\phi_{u}}{\phi_{y}},$$

(35)

where $\phi_{u}$ and $\phi_{y}$ are the ultimate and yield curvatures, respectively. Stress–strain relationship for the steel follows an elasto-plastic model and for concrete it was assumed an inelastic behavior [44]. In this application, the failure probability is calculated with respect to the following limit state function:

$$g(\mu_{\phi,\text{ini}}, \mu(\tau)) = \theta \mu_{\phi,\text{ini}} - \mu(\tau),$$

(36)

where $\theta \mu_{\phi,\text{ini}}$ corresponds to a fraction (i.e., $\theta$) of the initial ductility, $\mu_{\phi,\text{ini}}$, and $\mu(\tau)$ is the ductility of the pile at time $\tau$.

Three variations of the same limit state function were considered based on a fraction of the structural initial capacity, $\mu_{\phi,\text{ini}}, \theta$: (1) $\theta = 0.75$; (2) $\theta = 0.50$; and (3) $\theta = 0.25$. The probabilistic models of the variables used are shown in Table 5. The reliability was calculated by using a “point-in-time” analysis by using the first-order second-moment reliability method FOSM, which is conservative (upper bound) [45].

5.3. Results of the model

The failure probability of the three limit state functions for various average active biodeterioration rates ($\gamma_{av}$) is presented in Fig. 11. It can be observed that the shape of the fragility curves, i.e., slope and time to

<table>
<thead>
<tr>
<th>Variable</th>
<th>Distribution</th>
<th>Mean</th>
<th>Est. dev.</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>Load</td>
<td>Lognormal</td>
<td>400 kN</td>
<td>30 kN</td>
<td>Melchers [41]</td>
</tr>
<tr>
<td>$f'_{c}$</td>
<td>Normal</td>
<td>28 MPa</td>
<td>2.8 MPa</td>
<td>Melchers [41]</td>
</tr>
<tr>
<td>$f'_{y}$</td>
<td>Normal</td>
<td>420 MPa</td>
<td>42 MPa</td>
<td>Melchers [41]</td>
</tr>
<tr>
<td>$C_{th}$</td>
<td>Lognormal</td>
<td>0.37</td>
<td>0.04</td>
<td>Hong [42]</td>
</tr>
<tr>
<td>$C_{s}$</td>
<td>Lognormal</td>
<td>2</td>
<td>0.6</td>
<td>Luping and Andersen [40]</td>
</tr>
<tr>
<td>$D_{cl}$</td>
<td>Lognormal</td>
<td>$1.62 \times 10^{-6} \text{ cm}^2/\text{s}$</td>
<td>$0.5 \times 10^{-6} \text{ cm}^2/\text{s}$</td>
<td>Hong [42]</td>
</tr>
<tr>
<td>$\rho_{\text{rust}}$</td>
<td>Normal</td>
<td>3600 kg/m$^3$</td>
<td>360 kg/m$^3$</td>
<td>Thoft-Christensen [43]</td>
</tr>
<tr>
<td>$t_{\text{por}}$</td>
<td>Lognormal</td>
<td>$12.5 \times 10^{-6} \text{ m}$</td>
<td>$2.54 \times 10^{-6} \text{ m}$</td>
<td>Thoft-Christensen [43]</td>
</tr>
</tbody>
</table>
failure (i.e., $p_f = 1$) depend upon: (1) the average active biodeterioration rate and (2) the limit state function (i.e., defined as a fraction of the initial ductility $\theta$). Comparing the cases with and without biodeterioration, it is observed that the overall behavior is similar, but all failure times with biodeterioration occur earlier. In addition, as the average active biodeterioration rate grows, the time to failure decreases and the slope of the fragility curves increases. It can be observed also that the overall effect of $c_{av}$ is larger when the fraction of the initial ductility $\theta$ decreases.

Fig. 11. Fragility curves for various average active biodeterioration rates: (a) $\theta = 0.75$; (b) $\theta = 0.5$; and (c) $\theta = 0.25$.

Fig. 12. Relationship between average active biodeterioration rate and structural lifetime for the three limit states considered: $\theta = 0.75$; $\theta = 0.5$; and $\theta = 0.25$. 

...
The relationship between the average active biodeterioration rate and the time required to reach failure is plotted in Fig. 12. This figure shows that for all limit state functions, the time to failure grows as $c_{av}$ decreases. This time period also grows as $h$ decreases. For instance, for $\theta = 0.75$, the time to failure is 40 years for $c_{av} = 2.5$ mm/yr, and 80 years for $c_{av} = 0$ mm/yr, respectively. An inverse analysis can also be made from the data presented in Fig. 12; for a predefined life-cycle it is possible to estimate the average biodeterioration rate required to reach a given limit state. For example, if a time window of 60 years is selected, a $c_{av} = 0.9$ mm/yr is required to meet the failure limit condition as defined by a 75% of its initial curvature ductility (i.e., $(p_f)_{\theta=0.75} = 1$). The same values for $\theta = 0.5$ and $\theta = 0.25$ are $c_{av} = 1.3$ mm/yr and $c_{av} = 1.7$ mm/yr, respectively (Fig. 12).

Finally, it is important to notice the effect of deterioration in the reduction of the ductility capacity of the structural component. The change of ductility with time for a probability of failure equal to $p_f = 1$ and $p_f = 0.5$, and for various average biodeterioration rates is shown in Fig. 13. As expected, the ductility capacity decreases with time, but if biodeterioration is not considered, the structural ductility capacity is larger than in the case where this effect is included. For example, if biodeterioration is not taken into account, the time required to reach failure, for $\theta = 0.75$, will be 80 years. However, when considering biodeterioration, this time becomes $t(c_{av} = 0.5)_{\theta=0.75} = 69$ years (13%) and $t(c_{av} = 2.5)_{\theta=0.75} = 40$ years (50%). It is evident from the results that preventive maintenance against biodeterioration is paramount to extend the structural life.

6. Conclusions

Modeling the effects of biodeterioration in RC structures should to be explicitly included as part of infrastructure planning and design, in particular, when structures are located in aggressive environments. Biodeterioration might affect structural performance significantly causing an important reduction in the lifetime of the structure. The proposed model couples three processes: (1) steel corrosion; (2) concrete cracking; and (3) biodeterioration. This coupling process is used to compute the reduction of steel reinforcement area and concrete cross section as a function of time. Furthermore, a fuzzy inference system based on experimental data and expert opinions was used to model the biodeterioration rate which is an essential part of the integrated model. The fuzzy model is a very convenient tool which combines data bases with expert knowledge about the local environmental variables. The proposed model is illustrated by studying the effects of biodeterioration in the ductility capacity of sea port piles. A difference between 13% and 50% in the structural life was observed. The high variability is related to the value of $c_{av}$, which should be a subject of further experimental research.
### Appendix A. Glossary

<table>
<thead>
<tr>
<th>Term</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Aerobe</td>
<td>organisms that require oxygen for their vital processes</td>
</tr>
<tr>
<td>Aerotolerant anaerobes</td>
<td>organisms that not require oxygen, but are not affected by their exposure to air</td>
</tr>
<tr>
<td>Anaerobe</td>
<td>organisms that are unable to use oxygen for their vital processes</td>
</tr>
<tr>
<td>Autotroph</td>
<td>these are organisms that do not need organic carbon to survive because their carbon source is the inorganic CO₂ and some carbonates</td>
</tr>
<tr>
<td>Cell</td>
<td>fundamental unit of a living matter</td>
</tr>
<tr>
<td>Endolith</td>
<td>specie that lives inside the rocks or RC (thanks to previous perforations or cracks)</td>
</tr>
<tr>
<td>Heterotroph</td>
<td>unlike autotroph organisms, they need organic carbon for their survival</td>
</tr>
<tr>
<td>Hypha</td>
<td>any of the threadlike filaments forming the mycelium of a fungus</td>
</tr>
<tr>
<td>Microorganism</td>
<td>any organism of microscopic size</td>
</tr>
<tr>
<td>Mycelium</td>
<td>the vegetative part of a fungus consisting of a mass of branching threadlike hyphae</td>
</tr>
<tr>
<td>Mold or mould</td>
<td>a filamentous fungus that forms hypha and mycelium; produces a superficial growth on various kinds of damp or decaying organic matter</td>
</tr>
<tr>
<td>Organism</td>
<td>a living thing that has (or can develop) the ability to act or function independently</td>
</tr>
<tr>
<td>Yeast</td>
<td>unicellular fungi that reproduce mainly asexually by budding or division. Their cells are considerably larger than bacterial cells</td>
</tr>
</tbody>
</table>

### References


